


- ① a) Falso:  $\sqrt{2}$  es irracional y real, pues todos los  $n^{\circ}$  irracionales son reales.  
 b) Verdadero: todo entero puede escribirse en forma fraccionaria (de denominador 1, por ejemplo).  
 c) Falso: todos los  $n^{\circ}$  racionales son reales.  
 d) Falso: sólo son racionales los números obtenidos a partir del cociente de dos enteros.  
 e) Falso: el desarrollo decimal, o es periódico, o no lo es. Los conjuntos  $\mathbb{Q}$  e  $\mathbb{I}$  son mutuamente excluyentes.

- ② a)  $L = 2\pi r = 2\pi \cdot 2 = 4\pi$  Irracional.  
 b) hipotenusa =  $\sqrt{3^2 + 4^2} = 5$  Natural.  
 c) diagonal =  $\sqrt{2^2 + 2^2} = \sqrt{8}$  Irracional  
 d) área =  $2 \cdot 2 = 4$  Natural.  
 e)   $h = \sqrt{4^2 - 2^2} = \sqrt{12}$  Irracional.  
 f) área =  $\frac{1}{2} \cdot 4 \cdot 2\sqrt{3} = 4\sqrt{3}$  Irracional.  
 g) perímetro =  $4 + 4 + 4 = 12$  Natural.

- ③  $2'8383\dots \in \mathbb{Q}$  (racional);  $-\frac{3}{4} \in \mathbb{Q}$  (racional);  $-\frac{\sqrt{5}}{2} \in \mathbb{I}$  (irracional).  
 $\frac{1+\sqrt{5}}{2} \in \mathbb{I}$  (irracional);  $\sqrt[3]{8} + 2 = 4 \in \mathbb{N}$  (natural);  $\frac{\pi}{4} \in \mathbb{I}$  (irracional).  
 $-\frac{8}{4} = -2 \in \mathbb{Z}$  (entero);  $3'25 \in \mathbb{Q}$  (racional);  $\frac{1}{3} \in \mathbb{Q}$  (racional)  
 $\sqrt[4]{16} = \pm 2 \in \mathbb{Z}$  (entero);  $\sqrt[3]{-8} = -2 \in \mathbb{Z}$  (entero);  $1'020020002\dots \in \mathbb{I}$  (irracional).

④  $x = 5'21\bar{3}$  ;  $1000x = 5213'333\dots$   
 $100x = 521'333\dots$   
 $\hline 900x = 4692 \rightarrow x = \frac{4692}{900}$

$x = 3'8\bar{7}$  ;  $100x = 387'777\dots$   
 $10x = 38'777\dots$   
 $\hline 90x = 349 \rightarrow x = \frac{349}{90}$

$\left. \begin{array}{l} x = \frac{4692}{900} \\ x = \frac{349}{90} \end{array} \right\} \frac{4692}{900} - \frac{349}{90} = \frac{4692}{900} - \frac{3490}{900} = \frac{601}{450} = 1'33\bar{5}$

$$\textcircled{5} \text{ a) } \frac{13}{6} \approx 2'17 ; \quad \varepsilon_a = \left| 2'17 - \frac{13}{6} \right| = \left| \frac{217}{100} - \frac{13}{6} \right| = \left| \frac{651 - 650}{300} \right| = \frac{1}{300}$$

$$\varepsilon_r = \frac{1}{300} : \frac{13}{6} = \frac{6}{3900} \approx 0'00154 = 0'154 \%$$

$$\text{b) } \frac{17}{6} \approx 2'83 ; \quad \varepsilon_a = \left| \frac{17}{6} - 2'83 \right| = \left| \frac{17}{6} - \frac{283}{100} \right| = \left| \frac{850 - 849}{300} \right| = \frac{1}{300}$$

$$\varepsilon_r = \frac{1}{300} : \frac{17}{6} = \frac{6}{5100} \approx 0'00118 = 0'118 \%$$

$$\text{c) } \frac{32}{9} \approx 3'56 ; \quad \varepsilon_a = \left| 3'56 - \frac{32}{9} \right| = \left| \frac{356}{100} - \frac{32}{9} \right| = \left| \frac{3204 - 3200}{900} \right| = \frac{4}{900} = \frac{1}{225}$$

$$\varepsilon_r = \frac{1}{225} : \frac{32}{9} = \frac{9}{7200} \approx 0'00125 = 0'125 \%$$

$$\textcircled{6} \text{ a) } 1897'67 \approx 1900 ; \quad 987.514 \approx 987.500 ; \quad 123 \approx 100$$

$$\text{b) } 34'2345 \approx 34'235 ; \quad 0'8765 \approx 0'877 ; \quad 0'12345 \approx 0'123$$

$$\text{c) } \varepsilon = |1900 - 1897'67| = 2'33 ; \quad \varepsilon_r = \frac{2'33}{1897'67} \approx 0'00123 = 0'123 \%$$

$$\varepsilon = |987.500 - 987.514| = 14 ; \quad \varepsilon_r = \frac{14}{987514} \approx 1'42 \cdot 10^{-5} = 0'00142 \%$$

$$\varepsilon = |123 - 100| = 23 ; \quad \varepsilon_r = \frac{23}{123} \approx 0'187 = 18'7 \%$$

$$\textcircled{8} \text{ a) } 1^{\circ} \text{ telémetro: } \varepsilon_a = |14'48 - 14'39| = 0'09 \text{ m.}$$

$$\varepsilon_r = \frac{0'09}{14'39} = 0'625 \%$$

$$2^{\circ} \text{ telémetro: } \varepsilon_a = |7'85 - 7'92| = 0'07 \text{ m}$$

$$\varepsilon_r = \frac{0'07}{7'92} = 0'884 \%$$

b) Es más preciso el 1° telémetro, porque el error relativo es menor.

$$\textcircled{7} \quad \varepsilon_a < 0'0005 \text{ mm.}$$

$$\varepsilon_r < \frac{0'0005}{2'318 - 0'0005} \approx 2'16 \cdot 10^{-4} = 0'0216 \%$$

9)  $\sqrt{7} = 2.6457... \approx 2.65$

$\epsilon_a < 0.005$  ;  $\epsilon_r < \frac{0.005}{2.65 - 0.005} \approx 1.89 \cdot 10^{-3} = 0.189\%$

10)  $N = \frac{1}{10} + \frac{1}{10^3} + \frac{1}{10^6} + \frac{1}{10^{10}} + \frac{1}{10^{15}} + \dots = 0.1 + 0.001 + 0.000001 + 0.0000000001 +$

$+ 0.0000000000000001 + \dots = 0.101001000100001\dots$

Infinitas cifras decimales no periódicas, luego irracional.

11) a) Falso. Por ejemplo:

$$\begin{array}{r} 0.101001000100001\dots \quad (\text{irrac.}) \\ + 0.010110111011110\dots \quad (\text{irrac.}) \\ \hline \end{array}$$

$0.111111111111111\dots$  racional, por ser un decimal periódico.

b) Falso. Por ejemplo:

$$\left. \begin{array}{l} \sqrt{12} \text{ es irracional.} \\ \sqrt{3} \text{ es irracional} \end{array} \right\} \sqrt{12} \cdot \sqrt{3} = \sqrt{36} = \pm 6 \text{ entero.}$$

12) 9.08

13) a)  $5.83 \cdot 10^2$  ; b)  $4.66 \cdot 10^{-1}$  ; c)  $8.75 \cdot 10^{-3}$

14)  $3 \cdot 10^5 \frac{\text{km}}{\text{seg}} \cdot 8.31 \cdot 60 \text{ seg} = 1.4958 \cdot 10^8 \approx 1.50 \cdot 10^8 \text{ km.}$

15) Masa del sol =  $1.670 \cdot 10^{-24} \cdot 1.191 \cdot 10^{57} = 1.989 \cdot 10^{33} \text{ g} = 1.989 \cdot 10^{30} \text{ Kg}$

16) a)  $18 : 6.02 \cdot 10^{23} = 2.99 \cdot 10^{-23} \text{ g/molé.c.}$

b)  $12.7 \cdot 10^6 : 0.34 \cdot 10^7 = 3.74 \text{ veces mayor.}$

$$\textcircled{17} \text{ a) } \frac{a^{2x}}{a} = a^{2x-1}; \quad \text{b) } \frac{2^t \cdot 4^t}{8^{t-1}} = \frac{2^t \cdot 2^{2t}}{2^{3t-3}} = \frac{2^{3t}}{2^{3t-3}} = 2^{3t-3t+3} = 2^3 = 8;$$

$$\text{c) } (5^4)^{x-1} = 5^{4x-4}; \quad \text{d) } 10hk^3 \cdot 4h^4 = 40h^5k^3;$$

$$\text{e) } \frac{3^{x+1}}{3^{x-1}} = 3^{x+1-x+1} = 3^2 = 9$$

$$\textcircled{18} \text{ a) } (-3m^2n^2)^3 = -27m^6n^6; \quad \text{b) } (3b^2)^{-2} = \frac{1}{(3b^2)^2} = \frac{1}{9b^4}$$

$$\text{c) } \frac{(ab)^2}{b^{-1}} = (ab)^2 b = a^2 b^2 b = a^2 b^3$$

$$\text{d) } \left(\frac{m^3}{2n^2}\right)^4 = \frac{m^{12}}{16n^8}; \quad \text{e) } (2ab)^{-1} = \frac{1}{2ab}$$

$$\text{f) } 2(ab)^{-1} = \frac{2}{ab}; \quad \text{g) } 2ab^{-1} = \frac{2a}{b}$$

$$\text{h) } \left(\frac{-4a^3}{b}\right)^2 = \frac{16a^6}{b^2}$$

$$\textcircled{19} \quad 81 = 3^4; \quad 0.5 = \frac{1}{2} = 2^{-1}; \quad \frac{1}{25} = \frac{1}{5^2} = 5^{-2}; \quad \sqrt[3]{9} = \sqrt[3]{3^2} = 3^{2/3};$$

$$\frac{1}{\sqrt{2}} = \frac{1}{2^{1/2}} = 2^{-1/2}$$

$$\textcircled{20} \text{ a) } \frac{2^3 \cdot 5^{-7} \cdot 7^3}{2^{-4} \cdot 5^7 \cdot 7^{-3}} = 2^7 \cdot 5^{-14} \cdot 7^6$$

$$\text{b) } \frac{(a \cdot b)^2 (a^{-3} b^3)^3}{(a b^2 c^3)^{-5}} = \frac{a^2 b^2 a^{-9} b^9}{a^5 b^{-10} c^{-15}} = \frac{a^{-7} b^{11}}{a^5 b^{-10} c^{-15}} = a^{-12} b^{21} c^{15}$$

$$\textcircled{22} \text{ a) } \sqrt[4]{3^{-3}} = 3^{-3/4}; \quad \text{b) } \frac{1}{\sqrt[3]{4^2}} = \frac{1}{4^{2/3}} = 4^{-2/3} = 2^{-4/3}$$

$$\text{c) } a^3 \cdot \sqrt[3]{a^{-2}} = a^3 \cdot a^{-2/3} = a^{7/3}; \quad \text{d) } \frac{\sqrt[5]{2^3}}{\sqrt[3]{2^{-2}}} = \frac{2^{3/5}}{2^{-2/3}} = 2^{3/5+2/3} = 2^{19/15}$$

23) No es correcto:  $\sqrt{4 \cdot 25} \neq \sqrt{4} + \sqrt{0.25} = 2 + 0.5 = 2.5$

la raíz cuadrada de una suma No es la suma de las raíces cuadradas.

26) a)  $\frac{\sqrt{5}}{\sqrt{2}} = \frac{\sqrt{5}\sqrt{2}}{\sqrt{2}\sqrt{2}} = \frac{\sqrt{10}}{2}$

b)  $\frac{2+\sqrt{2}}{\sqrt{2}} = \frac{(2+\sqrt{2})\sqrt{2}}{\sqrt{2}\sqrt{2}} = \frac{2\sqrt{2}+2}{2} = \sqrt{2}+1$

c)  $\frac{3}{2-\sqrt{3}} = \frac{3(2+\sqrt{3})}{(2-\sqrt{3})(2+\sqrt{3})} = \frac{3(2+\sqrt{3})}{4-3} = 3(2+\sqrt{3}) = 6+3\sqrt{3}$

d)  $\frac{4}{\sqrt{3}+\sqrt{2}} = \frac{4(\sqrt{3}-\sqrt{2})}{(\sqrt{3}+\sqrt{2})(\sqrt{3}-\sqrt{2})} = \frac{4(\sqrt{3}-\sqrt{2})}{3-2} = 4(\sqrt{3}-\sqrt{2})$

e)  $\frac{1}{3\sqrt{2}-2\sqrt{3}} = \frac{3\sqrt{2}+2\sqrt{3}}{(3\sqrt{2}-2\sqrt{3})(3\sqrt{2}+2\sqrt{3})} = \frac{3\sqrt{2}+2\sqrt{3}}{18-12} = \frac{3\sqrt{2}+2\sqrt{3}}{6}$

28)  $\frac{(\sqrt[3]{a^2})^4 \cdot (a^2 \cdot \sqrt{a})^3}{\sqrt[6]{a^5}} = \frac{(a^{\frac{2}{3}})^4 \cdot (a^2 \cdot a^{\frac{1}{2}})^3}{a^{\frac{5}{6}}} = \frac{a^{\frac{8}{3}} \cdot a^6 \cdot a^{\frac{3}{2}}}{a^{\frac{5}{6}}} = \frac{a^{\frac{61}{6}}}{a^{\frac{5}{6}}}$

$= a^{\frac{56}{6}} = a^{\frac{28}{3}} = \sqrt[3]{a^{28}} = \sqrt[3]{a^{27} \cdot a} = a^9 \cdot \sqrt[3]{a}$

31) a)  $\sqrt{5} + \sqrt{45} + \sqrt{180} - \sqrt{80} = \sqrt{5} + 3\sqrt{5} + 6\sqrt{5} - 4\sqrt{5} = 6\sqrt{5}$

b)  $3\sqrt{72} - \sqrt{18} + 5\sqrt{2} + \sqrt{50} - 2\sqrt{8} = 18\sqrt{2} - 3\sqrt{2} + 5\sqrt{2} + 5\sqrt{2} - 4\sqrt{2} = 21\sqrt{2}$

c)  $9\sqrt{27} + 2\sqrt{3} - 8\sqrt{300} - 4\sqrt{3} = 27\sqrt{3} + 2\sqrt{3} - 80\sqrt{3} - 4\sqrt{3} = -55\sqrt{3}$

d)  $8\sqrt{8} - 5\sqrt{2} + 4\sqrt{20} - 12\sqrt{5} + 3\sqrt{18} = 16\sqrt{2} - 5\sqrt{2} + 8\sqrt{5} - 12\sqrt{5} + 9\sqrt{2} = 20\sqrt{2} - 4\sqrt{5}$

e)  $\sqrt[3]{-54} + 2 \cdot \sqrt[3]{16} = -3\sqrt[3]{2} + 4\sqrt[3]{2} = \sqrt[3]{2}$

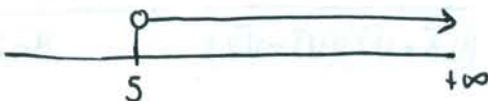
$$\begin{aligned} \textcircled{30} \quad \sqrt{\frac{5}{12}} - \sqrt{\frac{10}{6}} &= \frac{\sqrt{5}}{2\sqrt{3}} - \frac{\sqrt{10}}{\sqrt{6}} = \frac{\sqrt{5}\sqrt{3}}{2\sqrt{3}\sqrt{3}} - \frac{\sqrt{10}\cdot\sqrt{6}}{\sqrt{6}\cdot\sqrt{6}} = \frac{\sqrt{15}}{6} - \frac{\sqrt{60}}{6} = \\ &= \frac{\sqrt{15}-\sqrt{60}}{6} = \frac{\sqrt{15}-2\sqrt{15}}{6} = -\frac{\sqrt{15}}{6} \end{aligned}$$

$$\begin{aligned} \textcircled{32} \quad \sqrt[4]{9} + \sqrt{\frac{1}{3}} - \sqrt{\frac{4}{27}} &= \sqrt[4]{3^2} + \frac{1}{\sqrt{3}} - \frac{2}{3\sqrt{3}} = \sqrt{3} + \frac{1}{\sqrt{3}} - \frac{2}{3\sqrt{3}} = \\ &= \sqrt{3} + \frac{\sqrt{3}}{3} - \frac{2\sqrt{3}}{9} = \frac{9\sqrt{3} + 3\sqrt{3} - 2\sqrt{3}}{9} = \frac{10\sqrt{3}}{9} \Rightarrow \begin{cases} a=10 \\ b=9 \end{cases} \end{aligned}$$

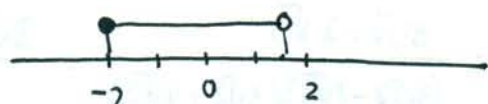
$\textcircled{33}$  a)  $[-3, 2]$



b)  $(5, +\infty)$



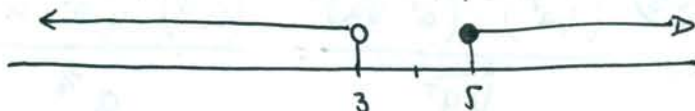
c)  $[-2, \frac{3}{2})$



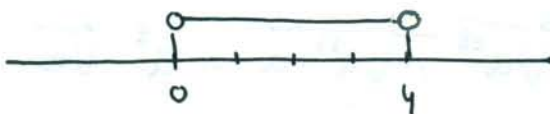
d)  $[-2, +\infty)$



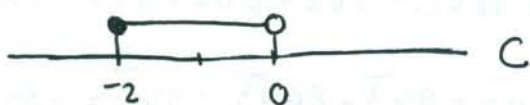
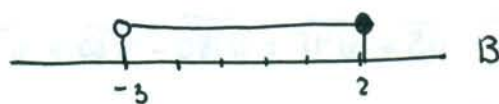
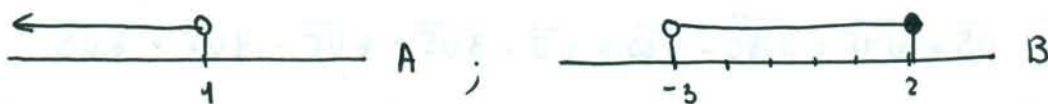
e)  $(-\infty, 3) \cup [5, +\infty)$



f)  $(0, 4)$



$\textcircled{34}$



$$A \cap B = (-3, 1); \quad A \cap C = [-2, 0); \quad A \cup B = (-\infty, 2]$$

$$A \cup C = (-\infty, 1); \quad A \cap B \cap C = [-2, 0)$$

④

$$\textcircled{35} \text{ a) } |2x| > 6 \Rightarrow \begin{cases} 2x > 6 \\ \sigma \\ 2x < -6 \end{cases} \Rightarrow \begin{cases} x > 3 \\ \sigma \\ x < -3 \end{cases} \Rightarrow (-\infty, -3) \cup (3, +\infty)$$

$$\text{b) } |2x-1| < 4 \Rightarrow -4 < 2x-1 < 4 \Rightarrow -3 < 2x < 5 \Rightarrow -\frac{3}{2} < x < \frac{5}{2} \\ \Rightarrow \left(-\frac{3}{2}, \frac{5}{2}\right)$$

$$\text{c) } |2x-6| = 4 \Rightarrow \begin{cases} 2x-6 = 4 \Rightarrow 2x = 10 \Rightarrow x = 5 \\ 2x-6 = -4 \Rightarrow 2x = 2 \Rightarrow x = 1 \end{cases}$$

$$\text{d) } |5x+2| = 8-x \Rightarrow \begin{cases} 5x+2 = 8-x \Rightarrow 6x = 6 \Rightarrow x = 1 \\ 5x+2 = -8+x \Rightarrow 4x = -10 \Rightarrow x = -\frac{5}{2} \end{cases}$$

$$\text{e) } |3x-8| < 10 \Rightarrow -10 < 3x-8 < 10 \Rightarrow -2 < 3x < 18 \Rightarrow -\frac{2}{3} < x < 6 \Rightarrow \\ \Rightarrow \left(-\frac{2}{3}, 6\right)$$

$$\text{f) } |4x+3| \leq 1 \Rightarrow -1 \leq 4x+3 \leq 1 \Rightarrow -4 \leq 4x \leq -2 \Rightarrow -1 \leq x \leq -\frac{1}{2} \\ \Rightarrow \left[-1, -\frac{1}{2}\right]$$

$$\text{g) } |2-x| > 0 \Rightarrow \begin{cases} 2-x > 0 \Rightarrow 2 > x \Rightarrow x < 2 \\ \sigma \\ 2-x < 0 \Rightarrow 2 < x \Rightarrow x > 2 \end{cases} \Rightarrow (-\infty, 2) \cup (2, +\infty) = \\ = \mathbb{R} - \{2\}$$

$$\text{h) } |1-3x| \leq 2 \Rightarrow -2 \leq 1-3x \leq 2 \Rightarrow -3 \leq -3x \leq 1 \Rightarrow \\ \Rightarrow -\frac{1}{3} \leq x \leq 1 \Rightarrow \left[-\frac{1}{3}, 1\right]$$

$$\text{i) } |-x| > 2 \Rightarrow \begin{cases} -x > 2 \Rightarrow x < -2 \\ \sigma \\ -x < -2 \Rightarrow x > 2 \end{cases} \Rightarrow (-\infty, -2) \cup (2, +\infty)$$

$$\text{j) } |2x-1| \leq \frac{1}{2} \Rightarrow -\frac{1}{2} \leq 2x-1 \leq \frac{1}{2} \Rightarrow \frac{1}{2} \leq 2x \leq \frac{3}{2} \Rightarrow \\ \Rightarrow \frac{1}{4} \leq x \leq \frac{3}{4} \Rightarrow \left[\frac{1}{4}, \frac{3}{4}\right]$$

$$\textcircled{21} \text{ a) } \left(\frac{27}{8}\right)^{\frac{2}{3}} = \left(\frac{3^3}{2^3}\right)^{\frac{2}{3}} = \frac{(3^3)^{\frac{2}{3}}}{(2^3)^{\frac{2}{3}}} = \frac{3^2}{2^2} = \frac{9}{4}$$

$$\text{b) } -125^{-\frac{1}{3}} = \frac{-1}{125^{\frac{1}{3}}} = \frac{-1}{(5^3)^{\frac{1}{3}}} = -\frac{1}{5}$$

$$\text{c) } \left(\frac{81}{16}\right)^{-\frac{3}{4}} = \left(\frac{3^4}{2^4}\right)^{-\frac{3}{4}} = \frac{(3^4)^{-\frac{3}{4}}}{(2^4)^{-\frac{3}{4}}} = \frac{3^{-3}}{2^{-3}} = \frac{2^3}{3^3} = \frac{8}{27}$$

$$\textcircled{24} \text{ a) } \sqrt[6]{27} = \sqrt[6]{3^3} = 3^{\frac{3}{6}} = 3^{\frac{1}{2}} = \sqrt{3}$$

$$\text{b) } \sqrt[6]{125} = \sqrt[6]{5^3} = 5^{\frac{3}{6}} = 5^{\frac{1}{2}} = \sqrt{5}$$

$$\text{c) } \frac{3\sqrt{512} + 5\sqrt{32}}{\sqrt{50} - \sqrt{18}} = \frac{3 \cdot 16\sqrt{2} + 5 \cdot 4\sqrt{2}}{5\sqrt{2} - 3\sqrt{2}} = \frac{48\sqrt{2} + 20\sqrt{2}}{5\sqrt{2} - 3\sqrt{2}} = \frac{68\sqrt{2}}{2\sqrt{2}} = 34$$

$$\textcircled{25} \text{ m.c.m}(2, 5, 15) = 30.$$

$$\sqrt{5} = \sqrt[30]{5^{15}}; \quad \sqrt[5]{2^3} = \sqrt[30]{2^{18}}; \quad \sqrt[15]{7^2} = \sqrt[30]{7^4}$$

$$\textcircled{27} \text{ a) } \frac{3}{\sqrt{6}} = \frac{3\sqrt{6}}{\sqrt{6} \cdot \sqrt{6}} = \frac{3\sqrt{6}}{6} = \frac{\sqrt{6}}{2}$$

$$\text{b) } \frac{6}{\sqrt[3]{2}} = \frac{6\sqrt[3]{2^2}}{\sqrt[3]{2} \cdot \sqrt[3]{2^2}} = \frac{6\sqrt[3]{4}}{\sqrt[3]{2^3}} = \frac{6\sqrt[3]{4}}{2} = 3\sqrt[3]{4}$$

$$\text{c) } \frac{\sqrt{27} + \sqrt{12}}{\sqrt{12} - \sqrt{3}} = \frac{(\sqrt{27} + \sqrt{12})(\sqrt{12} + \sqrt{3})}{(\sqrt{12} - \sqrt{3})(\sqrt{12} + \sqrt{3})} = \frac{\sqrt{324} + \sqrt{81} + \sqrt{144} + \sqrt{36}}{12 - 3} = \frac{18 + 9 + 12 + 6}{9} = \frac{45}{9} = 5$$



$$d) \frac{6}{\sqrt{7}+\sqrt{3}} = \frac{6(\sqrt{7}-\sqrt{3})}{(\sqrt{3}+\sqrt{7})(\sqrt{7}-\sqrt{3})} = \frac{6\sqrt{7}-6\sqrt{3}}{7-3} = \frac{6(\sqrt{7}-\sqrt{3})}{4} = \frac{3(\sqrt{7}-\sqrt{3})}{2} \quad (5)$$


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$$(29) \ a) \frac{\sqrt{27} \cdot \sqrt[5]{81}}{3^5 \cdot (\sqrt[3]{3})^4 \cdot 9^{-2}} = \frac{\sqrt{3^3} \cdot \sqrt[5]{3^4}}{3^5 \cdot \sqrt[3]{3^4} \cdot (3^2)^{-2}} = \frac{3^{\frac{3}{2}} \cdot 3^{\frac{4}{5}}}{3^5 \cdot 3^{\frac{4}{3}} \cdot 3^{-4}} =$$

$$= \frac{3^{\frac{15}{10}} \cdot 3^{\frac{4}{10}}}{3 \cdot 3^{\frac{4}{3}}} = \frac{3^{\frac{19}{10}}}{3^{\frac{7}{3}}} = 3^{\frac{19}{10} - \frac{7}{3}} = 3^{\frac{57-70}{30}} = 3^{-\frac{13}{30}}$$

$$b) \frac{2^{\frac{3}{2}} \cdot 8^0 \cdot 4^{-\frac{1}{3}}}{2^{-1} \cdot \sqrt[3]{2}} = \frac{2^{\frac{3}{2}} \cdot 1 \cdot 2^{-\frac{2}{3}}}{2^{-1} \cdot 2^{\frac{1}{3}}} = \frac{2^{\frac{9-4}{6}}}{2^{-\frac{2}{3}}} = \frac{2^{\frac{5}{6}}}{2^{-\frac{2}{3}}} = 2^{\frac{5}{6} + \frac{2}{3}} =$$

$$= 2^{\frac{5+4}{6}} = 2^{\frac{9}{6}} = 2^{\frac{3}{2}}$$


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