

ECUACIONES, INECUACIONES Y SISTEMAS.

② a) $x^2 - 6x = 11$; $x^2 - 6x + 9 = 11 + 9$; $(x-3)^2 = 20$; $x-3 = \pm\sqrt{20} \Rightarrow x = 3 \pm 2\sqrt{5}$

b) $x^2 - 2x = 5$; $x^2 - 2x + 1 = 5 + 1$; $(x-1)^2 = 6$; $x-1 = \pm\sqrt{6} \Rightarrow x = 1 \pm \sqrt{6}$

c) $x^2 + x = 42$; $x^2 + x + \frac{1}{4} = 42 + \frac{1}{4}$; $(x + \frac{1}{2})^2 = \frac{169}{4}$; $x + \frac{1}{2} = \pm \frac{13}{2} \Rightarrow$

$\Rightarrow x = -\frac{1}{2} \pm \frac{13}{2} = \begin{cases} 6 \\ -7 \end{cases}$

d) $2(x^2 - 2x - \frac{9}{2}) = 0$; $x^2 - 2x = \frac{9}{2}$; $x^2 - 2x + 1 = \frac{9}{2} + 1$; $(x-1)^2 = \frac{11}{2}$; $x-1 = \pm\sqrt{\frac{11}{2}}$

$\Rightarrow x = 1 \pm \frac{\sqrt{11}}{\sqrt{2}} = 1 \pm \frac{\sqrt{22}}{2}$

e) $x^2 - 4x = -12$; $x^2 - 4x + 4 = -12 + 4$; $(x-2)^2 = -8$; $x-2 = \pm\sqrt{-8}$ \nexists sol. real.

f) $x^2 + 5x = 84$; $x^2 + 5x + \frac{25}{4} = 84 + \frac{25}{4}$; $(x + \frac{5}{2})^2 = \frac{361}{4}$; $x + \frac{5}{2} = \pm \frac{19}{2} \Rightarrow$

$\Rightarrow x = -\frac{5}{2} \pm \frac{19}{2} = \begin{cases} 7 \\ -12 \end{cases}$

③ a) $x(3x+2) = 0 \Rightarrow \begin{cases} x=0 \\ x=-\frac{2}{3} \end{cases}$

b) $5x^2 = 20 \Rightarrow x^2 = 4 \Rightarrow x = \pm 2$

c) $3x^2 - 9x = 30 \Rightarrow x^2 - 3x = 10$; $x^2 - 3x + \frac{9}{4} = 10 + \frac{9}{4}$; $(x - \frac{3}{2})^2 = \frac{49}{4}$;

$x - \frac{3}{2} = \pm \frac{7}{2} \Rightarrow x = \frac{3}{2} \pm \frac{7}{2} = \begin{cases} 5 \\ -2 \end{cases}$

d) $10x^2 + 15x - 8x - 12 = 5$; $10x^2 + 7x - 17 = 0 \Rightarrow x = \frac{-7 \pm \sqrt{49 + 680}}{20} = \frac{-7 \pm 27}{20}$

$= \begin{cases} 1 \\ -\frac{34}{20} = -\frac{17}{10} \end{cases}$

e) $7x - x^2 = 0 \Rightarrow x(7-x) = 0 \begin{cases} \nearrow x=0 \\ \searrow x=7 \end{cases}$

$16x^2 - 9 = 0 \Rightarrow x^2 = \frac{9}{16} \Rightarrow x = \pm \frac{3}{4}$

f) $4x^2 + 4x + 1 + 6x + 3 = 0 \Rightarrow 4x^2 + 10x + 4 = 0 \Rightarrow 2x^2 + 5x + 2 = 0 \Rightarrow$

$\Rightarrow x = \frac{-5 \pm \sqrt{25 - 16}}{4} = \frac{-5 \pm 3}{4} = \begin{cases} -2 \\ -\frac{1}{2} \end{cases}$

$$g) x^4 - 13x^2 + 36 = 0 ; x^2 = t \Rightarrow t^2 - 13t + 36 = 0 \Rightarrow t = \frac{13 \pm \sqrt{169 - 144}}{2} = \begin{cases} 9 \\ 4 \end{cases}$$

$$t = 9 \Rightarrow x = \pm \sqrt{9} = \pm 3$$

$$t = 4 \Rightarrow x = \pm \sqrt{4} = \pm 2$$

$$h) x^2 + 1 = \frac{1}{x^2} \Rightarrow x^4 + x^2 = 1 \Rightarrow x^4 + x^2 - 1 = 0 ; x^2 = t \Rightarrow t^2 + t - 1 = 0$$

$$\Rightarrow t = \frac{-1 \pm \sqrt{1+4}}{2} = \frac{-1 \pm \sqrt{5}}{2} = \begin{cases} \frac{-1+\sqrt{5}}{2} = 0.6180339... \Rightarrow x = \pm 0.786 \\ \frac{-1-\sqrt{5}}{2} = -1.6180339... \Rightarrow \text{No sol. real para } x. \end{cases}$$

$$i) \frac{9x+15}{12} - \frac{8x+20}{12} = \frac{x^2-6x+5}{12} \Rightarrow 9x+15-8x-20 = x^2-6x+5 \Rightarrow$$

$$\Rightarrow x^2 - 7x + 10 = 0 \Rightarrow x = \begin{cases} 2 \\ 5 \end{cases}$$

$$j) x^3 = t \Rightarrow t^2 - 28t + 27 = 0 \Rightarrow t = \begin{cases} 1 \Rightarrow x = \sqrt[3]{1} = 1 \\ 27 \Rightarrow x = \sqrt[3]{27} = 3 \end{cases}$$

$$\textcircled{4} a) \Delta = 0 \Rightarrow 64 - 4 \cdot 3 \cdot (-3k) = 0 \Rightarrow 64 + 36k = 0 \Rightarrow 36k = -64 \Rightarrow k = \frac{-64}{36} = \frac{-16}{9}$$

$$b) 4(k+1)^2 - 4 \cdot (k-1) \cdot k = 0 \Rightarrow 4k^2 + 8k + 4 - 4k^2 + 4k = 0 \Rightarrow 12k = -4 \Rightarrow k = \frac{-1}{3}$$

NO

$$\begin{cases} a) p^2 - 4 > 0 \Rightarrow p^2 > 4 \Rightarrow p > 2 \text{ o } p < -2 \Rightarrow (-\infty, -2) \cup (2, +\infty) \\ b) p^2 - 4 = 0 \Rightarrow p = \pm 2 \\ c) p^2 - 4 < 0 \Rightarrow p \in (-2, 2) \end{cases}$$

$$\textcircled{5} 16k^2 - 4 \cdot 4 \cdot 9 = 0 \Rightarrow 16k^2 - 144 = 0 \Rightarrow k^2 = 9 \Rightarrow k = 3 \text{ (sólo la +)}$$

$$\textcircled{7} k^2 - 36 > 0 \Rightarrow k^2 > 36 \Rightarrow k > 6 \text{ o } k < -6 ; \text{ luego:}$$

$$k \in (-\infty, -6) \cup (6, +\infty)$$

$$\textcircled{8} a) (k-3)^2 - 4k = 0 \Rightarrow k^2 - 6k + 9 - 4k = 0 \Rightarrow k^2 - 10k + 9 = 0 \Rightarrow k = \begin{cases} 1 \\ 9 \end{cases}$$

$$b) k = 1 \text{ o } k = 9$$

11) a) $28 + 2x = 16 + x + 8\sqrt{x} \Rightarrow 12 + x = 8\sqrt{x} \Rightarrow (12+x)^2 = 64x \Rightarrow$

$\Rightarrow 144 + 24x + x^2 = 64x \Rightarrow x^2 - 40x + 144 = 0 \Rightarrow x = \begin{cases} 4 & \checkmark \\ 36 & \checkmark \end{cases}$

b) $\sqrt{2x-1} = 6 - \sqrt{x+4}; 2x-1 = 36 + x + 4 - 12\sqrt{x+4} \Rightarrow$

$\Rightarrow x - 41 = -12\sqrt{x+4} \Rightarrow (x-41)^2 = 144(x+4) \Rightarrow x^2 - 82x + 1681 = 144x + 576;$

$x^2 - 226x + 1105 = 0 \Rightarrow x = \begin{cases} 5 & \checkmark \\ 221 & \text{(No válida).} \end{cases}$

c) $1 + \sqrt{2+\sqrt{x}} = 9 \Rightarrow \sqrt{2+\sqrt{x}} = 8 \Rightarrow 2+\sqrt{x} = 64 \Rightarrow \sqrt{x} = 62 \Rightarrow$

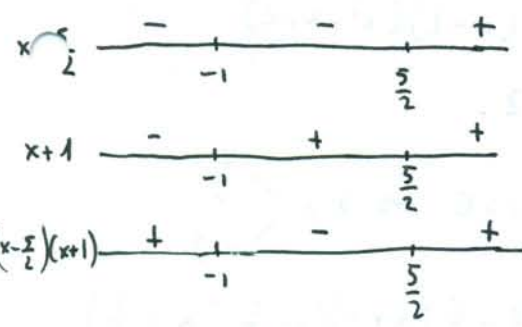
$\Rightarrow x = 62^2 \Rightarrow x = 3844 \checkmark$

d) $2 + \sqrt{x-5} = 13 - x \Rightarrow \sqrt{x-5} = 11 - x \Rightarrow x-5 = 121 - 22x + x^2 \Rightarrow$

$\Rightarrow x^2 - 23x + 126 = 0 \Rightarrow x = \begin{cases} 9 & \checkmark \\ 14 & \text{(No válida).} \end{cases}$

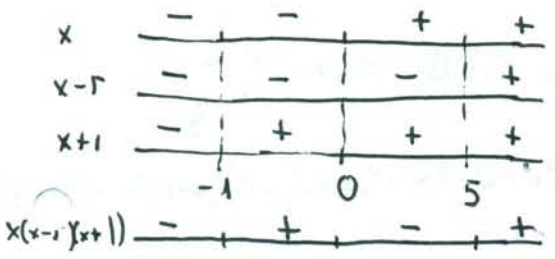
15) a) $x^2 - 3x - 1 < x^2 + x - 2 \Rightarrow -4x < -1 \Rightarrow 4x > 1 \Rightarrow x > \frac{1}{4}$

b) $-2x^2 + 3x + 5 \geq 0 \Rightarrow 2x^2 - 3x - 5 \leq 0 \Rightarrow 2(x - \frac{5}{2})(x + 1) \leq 0$



Sol: $x \in [-1, \frac{5}{2}]$

c) $x^3 - 4x^2 - 5x > 0 \Rightarrow x(x^2 - 4x - 5) > 0 \Rightarrow x(x-5)(x+1) > 0$



Sol: $(-1, 0) \cup (5, +\infty)$

$$d) x^2 - 5x + 4 \geq 0 \Rightarrow (x-1)(x-4) \geq 0$$

$x-1$	-	1	+	4	+
$x-4$	-		-		+
$(x-1)(x-4)$	+		-		+

$$\text{Sol: } (-\infty, 1] \cup [4, +\infty)$$

$$16) a) \frac{x+4}{(x-3)(x+3)} < 0$$

$x+4$	-	-4	+	-3	+	3	+
$x-3$	-		-		-		+
$x+3$	-		-		+		+
$\frac{x+4}{(x-3)(x+3)}$	-		+		-		+

$$\text{Sol: } (-\infty, -4) \cup (-3, 3)$$

$$b) \frac{2-x}{x+3} < 2 \Rightarrow \frac{2-x}{x+3} - 2 < 0 \Rightarrow \frac{2-x-2x-6}{x+3} < 0 \Rightarrow$$

$$\Rightarrow \frac{-3x-4}{x+3} < 0$$

$-3x-4$	+	-3	+	-4/3	-
$x+3$	-		+		+
$\frac{-3x-4}{x+3}$	-		+		-

$$\text{Sol: } (-\infty, -3) \cup (-\frac{4}{3}, +\infty)$$

$$17) a) \begin{array}{r|rrrr} 1 & 1 & -1 & 0 & -4 \\ & 2 & 2 & 2 & 4 \\ \hline & 1 & 1 & 2 & 0 \end{array}$$

$$x^2 + x + 2 = 0 \Rightarrow \text{no real sol.}$$

$$x^3 - x^2 - 4 = (x-2)(x^2 + x + 2)$$

$$\text{Sol: } x = 2.$$

$$b) \begin{array}{r|rrrr} 6 & 6 & 1 & -26 & -21 \\ & -1 & -6 & 5 & 21 \\ \hline & 6 & -5 & -21 & 0 \end{array}$$

$$6x^2 - 5x - 21 = 0 \Rightarrow x = \begin{cases} \frac{7}{3} \\ -\frac{3}{2} \end{cases}$$

$$6x^3 + x^2 - 26x - 21 = 6(x+1)(x-\frac{7}{3})(x+\frac{3}{2})$$

$$\text{Sol: } x = -1; \frac{7}{3}; -\frac{3}{2}$$

$$c) \begin{array}{r|rrrrr} 6 & 6 & -17 & 7 & 8 & -4 \\ & 1 & 6 & -11 & -4 & 4 \\ \hline & 6 & -11 & -4 & 4 & 0 \\ & 2 & 12 & 2 & -4 & \\ \hline & 6 & 1 & -2 & 0 & \end{array}$$

$$6x^2 + x - 2 = 0 \Rightarrow x = \begin{cases} \frac{1}{2} \\ -\frac{2}{3} \end{cases}$$

$$6x^4 - 17x^3 + 7x^2 - 8x - 4 = 6(x-1)(x-2)(x-\frac{1}{2})(x+\frac{2}{3})$$

$$\text{Sol: } x = 1; 2; \frac{1}{2}; -\frac{2}{3}$$

$$d) \begin{array}{r|rrrrr} 1 & 1 & -2 & -10 & 4 & 16 \\ & -2 & -2 & 8 & 4 & -16 \\ \hline & 1 & -4 & -2 & 8 & 0 \\ & 4 & 4 & 0 & -8 & \\ \hline & 1 & 0 & -2 & 0 & \end{array}$$

$$x^2 - 2 = 0 \Rightarrow x^2 = 2 \Rightarrow x = \pm \sqrt{2}$$

$$x^4 - 2x^3 - 10x^2 + 4x + 16 = (x+2)(x-4)(x-\sqrt{2})(x+\sqrt{2})$$

Sol: $x = -2; 4; \sqrt{2}; -\sqrt{2}$.

NO $\left\{ \begin{array}{l} \text{Luego, los números son: } 7x = 7 \cdot 13 = 91 \text{ y } 7x+7 = 98, \text{ o bien:} \\ 7x = 7 \cdot (-14) = -98 \text{ y } 7x+7 = -91. \end{array} \right.$

20) $60 + 4 \cdot 5x < 600 \Rightarrow x < 120$: por debajo de 120 h. de programación es más interesante la 1ª empresa.

21) $S = \frac{x \cdot 3x}{2} = \frac{3x^2}{2} > 37 \cdot 5 \Rightarrow x > 5$

22) $x - 3 = \sqrt{x+3} \Rightarrow x = 6$

23) $(24+x)^2 = (22+x)^2 + (8+x)^2 \Rightarrow x = 2$; luego las medidas son: 10, 24, 26.

24) $x^3 = (x-3)^3 + (x-2)^3 + (x-1)^3 \Rightarrow x = 6$ (ec. polinómica de grado 3).

25) $\left. \begin{array}{l} 0'05A + 0'10B = 10 \\ 0'03A + 0'01B = 3 \end{array} \right\} \begin{array}{l} 5A + 10B = 1000 \\ 3A + B = 300 \end{array} \left\} \begin{array}{l} A + 2B = 200 \\ 3A + B = 300 \end{array} \right\} \Rightarrow$

$$\begin{array}{r} A + 2B = 200 \\ -6A - 2B = -600 \\ \hline -5A = -400 \end{array} \Rightarrow \begin{array}{l} A = 80 \text{ g.} \\ B = 300 - 3A \Rightarrow B = 60 \text{ g.} \end{array}$$

$$\begin{array}{l} \textcircled{29} \quad x = n^{\circ} \text{ ejemplares} \\ \quad \quad y = \text{precio/ejemplar} \end{array} \left\{ \begin{array}{l} x \cdot y = 252 \\ (x-4)(y+0'3) = 252 \end{array} \right. \left. \begin{array}{l} x \cdot y = 252 \\ xy + 0'3x - 4y - 1'2 = 252 \end{array} \right.$$

$$\Rightarrow \cancel{252} + 0'3x - 4y - 1'2 = \cancel{252} \Rightarrow 0'3x - 4y = 1'2 ; \quad y = \frac{252}{x} \Rightarrow$$

$$\Rightarrow 0'3x - 4 \cdot \frac{252}{x} = 1'2 \Rightarrow 0'3x - \frac{1008}{x} = 1'2 \Rightarrow 0'3x^2 - 1008 = 1'2x$$

$$\Rightarrow 0'3x^2 - 1'2x - 1008 = 0 \Rightarrow x = \begin{array}{l} 60 \\ -56 \end{array} \quad (\text{sin sentido en el contexto del problema})$$

luego: $x = 60$ ejemplares.

$$y = \frac{252}{60} = 4'2 \text{ € / ejemplar.}$$

$$\textcircled{30} \quad \left. \begin{array}{l} 240x = y \\ 300(x-3) = y \end{array} \right\} \begin{array}{l} (\text{riendo } x = n^{\circ} \text{ vecinos ; } y = \text{precio de la obra}). \\ \text{Sol: } x = 15 \text{ vecinos ; } y = 3600 \text{ €}. \end{array}$$

$$\textcircled{31} \quad \left. \begin{array}{l} x = n^{\circ} \text{ turistas} \\ y = \text{coste/persona} \end{array} \right\} \begin{array}{l} x \cdot y = 36000 \\ (x-6)(y+225) = 0'95 \cdot 36000 \end{array} \left. \begin{array}{l} x = 30 \text{ pers.} \\ y = 1200 \text{ €}. \end{array} \right.$$

(Resolución similar al sistema del ejercicio ²⁹).

$$\textcircled{1} \quad \text{a) } \frac{3}{4}(2x-4) = x-5 \Rightarrow 3(2x-4) = 4(x-5) \Rightarrow 6x-12 = 4x-20$$

$$\Rightarrow 6x-4x = 12-20 \Rightarrow 2x = -8 \Rightarrow \boxed{x = -4}$$

$$\text{b) } \frac{x-1}{4} - \frac{x-5}{36} = \frac{x+5}{9} \Rightarrow \frac{9x-9}{36} - \frac{x-5}{36} = \frac{4x+20}{36} \Rightarrow$$

$$\Rightarrow 9x-9-x+5 = 4x+20 \Rightarrow 9x-x-4x = 20+9-5 \Rightarrow 4x = 24 \Rightarrow \boxed{x = 6}$$

$$\text{c) } 6\left(\frac{1}{8} - \frac{2x-3}{16}\right) - \frac{9}{4}x = \frac{9x-6}{8} \Rightarrow \frac{6}{8} - \frac{12x-18}{16} - \frac{9}{4}x = \frac{9x-6}{8} \Rightarrow$$

$$\rightarrow 12 - 12x + 18 - 36x = 18x - 12 \Rightarrow -12x - 36x - 18x = -12 - 12 - 18 \quad (4)$$

$$\Rightarrow -66x = -42 \Rightarrow x = \frac{42}{66} = \boxed{\frac{7}{11} = x}$$

$$(3) \text{ k) } 4x^4 - 37x^2 + 9 = 0 \Rightarrow x^2 = t \Rightarrow 4t^2 - 37t + 9 = 0 \Rightarrow$$

$$\Rightarrow t = \frac{37 \pm \sqrt{1369 - 4 \cdot 4 \cdot 9}}{2 \cdot 4} = \frac{37 \pm 35}{8} = \begin{cases} 9 & \Rightarrow x = \pm \sqrt{9} = \pm 3 \\ \frac{1}{4} & \Rightarrow x = \pm \sqrt{\frac{1}{4}} = \pm \frac{1}{2} \end{cases}$$

$$\text{l) } 25x^2(x^2 - 1) + 11(x^4 + 1) - 7 = 0 \Rightarrow 25x^4 - 25x^2 + 11x^4 + 11 - 7 = 0$$

$$\Rightarrow 36x^4 - 25x^2 + 4 = 0 \Rightarrow x^2 = t \Rightarrow 36t^2 - 25t + 4 = 0 \Rightarrow$$

$$\Rightarrow t = \frac{25 \pm \sqrt{625 - 4 \cdot 36 \cdot 4}}{2 \cdot 36} = \frac{25 \pm 7}{72} = \begin{cases} \frac{32}{72} = \frac{4}{9} & \Rightarrow x = \pm \sqrt{\frac{4}{9}} = \pm \frac{2}{3} \\ \frac{18}{72} = \frac{1}{4} & \Rightarrow x = \pm \sqrt{\frac{1}{4}} = \pm \frac{1}{2} \end{cases}$$

$$(6) \Delta = 9 - 4K = 0 \Rightarrow 9 = 4K \Rightarrow K = \frac{9}{4}$$

$$(9) \Delta = (K-1)^2 - 4 = 0 \Rightarrow (K-1)^2 = 4 \Rightarrow K-1 = \pm 2 \Rightarrow K = \begin{cases} 1+2=3 \\ 1-2=-1 \end{cases}$$

$$(10) \Delta = 9 - 4K^2 > 0 \Rightarrow (3-2K)(3+2K) > 0 \Rightarrow K = \pm \frac{3}{2}$$

$$\begin{array}{c} 3-2K \quad + \quad -\frac{3}{2} \quad + \quad \frac{3}{2} \quad - \\ 3+2K \quad - \quad + \quad - \quad + \end{array}$$

$$(3-2K)(3+2K) \quad - \quad + \quad -$$

$$\Rightarrow K \in \left(-\frac{3}{2}, \frac{3}{2}\right)$$

$$(11) \text{ e) } x - \sqrt{25-x^2} = 1 \Rightarrow x-1 = \sqrt{25-x^2} \Rightarrow (x-1)^2 = 25-x^2 \Rightarrow$$

$$\Rightarrow x^2 - 2x + 1 = 25 - x^2 \Rightarrow 2x^2 - 2x - 24 = 0 \Rightarrow x^2 - x - 12 = 0 \Rightarrow$$

$$\rightarrow x = \begin{cases} -3 & \text{No válida.} \\ 4 & \checkmark \end{cases}$$

$$f) \sqrt{7+2x} - \sqrt{3+x} = 1 \Rightarrow \sqrt{7+2x} = 1 + \sqrt{3+x} \Rightarrow$$

$$\Rightarrow 7+2x = 1 + 3+x + 2\sqrt{3+x} \Rightarrow 3+x = 2\sqrt{3+x} \Rightarrow$$

$$\Rightarrow 9+x^2+6x = 4(3+x) \Rightarrow 9+x^2+6x = 12+4x \Rightarrow x^2+2x-3=0$$

$$\Rightarrow x = \begin{cases} 1 & \checkmark \\ -3 & \checkmark \end{cases}$$

$$(12) a) \frac{2-x}{2} + \frac{4}{x+2} = 1 \Rightarrow \frac{(2-x)(x+2) + 8}{2(x+2)} = 1 \Rightarrow$$

$$\Rightarrow (2-x)(2+x) + 8 = 2(x+2) \Rightarrow \cancel{4} - x^2 + 8 = 2x + \cancel{4} \Rightarrow x^2 + 2x - 8 = 0$$

$$\Rightarrow x = \begin{cases} 2 & \checkmark \\ -4 & \checkmark \end{cases}$$

$$b) x - \frac{9}{x} = \frac{3}{x} - 1 \Rightarrow \frac{x^2-9}{x} = \frac{3-x}{x} \Rightarrow x^3-9x = 3x-x^2$$

$$\Rightarrow x^3+x^2-12x=0 \Rightarrow x(x^2+x-12)=0 \Rightarrow x = \begin{cases} 0 & \text{(No valida)} \\ 3 & \checkmark \\ -4 & \checkmark \end{cases}$$

$$(13) a) \begin{cases} 2x+3y=3 \\ 5x+7y=8 \end{cases} \begin{cases} 10x+15y=15 \\ -10x-14y=-16 \end{cases} \begin{matrix} 2x-3=3 \\ 2x=6 \Rightarrow \boxed{x=3} \end{matrix}$$

$$\boxed{y=-1}$$

$$b) \begin{cases} x + \frac{6}{y} = 2 \\ 3x - y = -5 \end{cases} \begin{matrix} y = 3x + 5 \\ x + \frac{6}{3x+5} = 2 \Rightarrow \frac{x(3x+5) + 6}{3x+5} = 2 \end{matrix}$$

$$\Rightarrow 3x^2+5x+6 = 6x+10 \Rightarrow 3x^2-x-4=0 \Rightarrow x = \begin{cases} \frac{4}{3} \\ -1 \end{cases}$$

$$\text{Si } x = \frac{4}{3} \Rightarrow y = 3 \cdot \frac{4}{3} + 5 = 9$$

$$\text{Si } x = -1 \Rightarrow y = -3 + 5 = 2.$$

$$c) \begin{cases} x^2 + y = 3 \\ 2x - y = 5 \end{cases} \Rightarrow y = 2x - 5 \Rightarrow x^2 + 2x - 5 = 3 \Rightarrow x^2 + 2x - 8 = 0 \Rightarrow x = \begin{cases} 2 \\ -4 \end{cases}$$

si $x = 2 \Rightarrow y = 4 - 5 = -1$
 si $x = -4 \Rightarrow y = -8 - 5 = -13$.

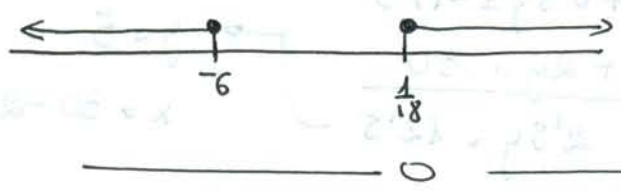
$$(14) \frac{5}{6}(3-x) - \frac{1}{2}(x-4) \geq \frac{2x-3}{3} - x \Rightarrow \frac{15-5x}{6} - \frac{x-4}{2} \geq \frac{2x-3}{3} - x$$

$$\Rightarrow 15 - 5x - 3x + 12 \geq 4x - 6 - 6x \Rightarrow -8x + 27 \geq -2x - 6 \Rightarrow -6x \geq -33$$

$$\Rightarrow 6x \leq 33 \Rightarrow x \leq \frac{33}{6} = \frac{11}{2} \Rightarrow x \in (-\infty, \frac{11}{2}]$$

$$(18) \begin{cases} \frac{2}{3} - x \leq 2x + \frac{1}{2} \\ \frac{x}{3} - \frac{2-x}{2} \geq x \end{cases} \Rightarrow \begin{cases} 4 - 6x \leq 12x + 3 \\ 2x - 6 + 3x \geq 6x \end{cases} \Rightarrow \begin{cases} -18x \leq -1 \\ -x \geq 6 \end{cases} \Rightarrow \begin{cases} 18x \geq 1 \\ x \leq -6 \end{cases}$$

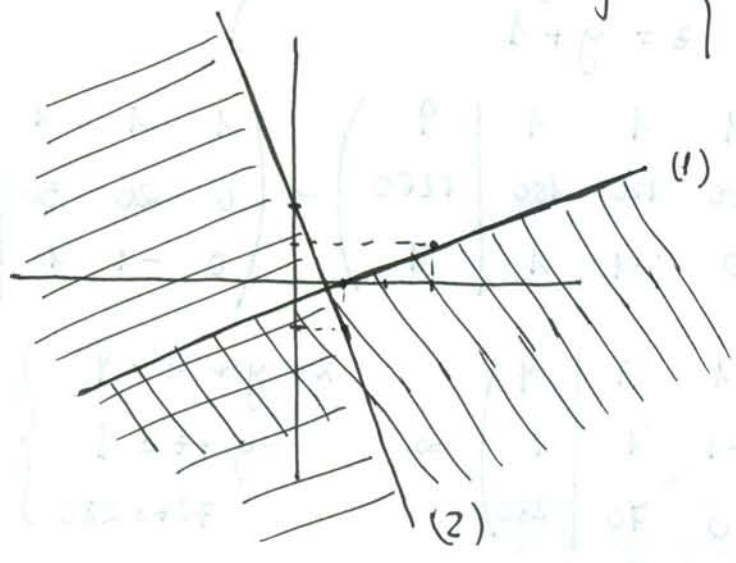
$$\left. \begin{matrix} x \geq \frac{1}{18} \\ x \leq -6 \end{matrix} \right\}$$



∅ solución (no hay puntos comunes)

$$(19) \begin{cases} x - 2y < 1 \\ 3x + y \geq 2 \end{cases} \Rightarrow \begin{cases} x - 2y = 1 \\ 3x + y = 2 \end{cases} \Rightarrow \begin{cases} x = 3; y = 1 \Rightarrow (3, 1) \\ y = 0; x = 1 \Rightarrow (1, 0) \end{cases} \quad (1)$$

$$\Rightarrow \begin{cases} 3x + y = 2 \\ y = -1; x = 1 \Rightarrow (1, -1) \end{cases} \quad (2)$$



26 $x \rightarrow$ edad de Ana
 $y \rightarrow$ edad de Benito

$$\begin{cases} 2x + y = 44 \\ x + 2 = 2(y + 2) \end{cases} \Rightarrow \begin{cases} 2x + y = 44 \\ x + 2 = 2y + 4 \end{cases}$$

$$\begin{cases} 2x + y = 44 \\ x - 2y = 2 \end{cases} \Rightarrow \begin{cases} 4x + 2y = 88 \\ x - 2y = 2 \end{cases}$$

$$\hline 5x = 90$$

$$x = \frac{90}{5} = 18; \quad y = 44 - 2x = 44 - 2 \cdot 18 = 8$$

27 $\begin{cases} \frac{x+3}{y+5} = \frac{2}{3} \\ \frac{x-2}{y-1} = \frac{1}{2} \end{cases} \Rightarrow \begin{cases} 3x+9 = 2y+10 \\ 2x-4 = y-1 \end{cases} \Rightarrow \begin{cases} 3x-2y = 1 \\ 2x-y = 3 \end{cases}$

$$\begin{cases} 3x-2y = 1 \\ -4x+2y = -6 \end{cases} \Rightarrow \hline -x = -5$$

$\Rightarrow x = 5 \quad y = 2x - 3 \Rightarrow y = 7 \Rightarrow \boxed{\frac{5}{7}}$

28 $x \rightarrow$ n° respuestas correctas
 $y \rightarrow$ n° respuestas equivocadas

$$\begin{cases} x - 0'5y = 17'5 \\ x + 2y = 30 \end{cases} \Rightarrow \begin{cases} -x + 0'5y = -17'5 \\ x + 2y = 30 \end{cases}$$

$$\hline 2'5y = 12'5 \Rightarrow y = 5$$

$$x = 30 - 2y = 30 - 10 = 20$$

32 $x \rightarrow$ n° Kg patatas
 $y \rightarrow$ n° Kg manzanas
 $z \rightarrow$ n° Kg uvas

$$\begin{cases} x + y + z = 9 \\ 100x + 120y + 150z = 1160 \\ -y + z = 1 \end{cases} \Rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 9 \\ 100 & 120 & 150 & 1160 \\ 0 & -1 & 1 & 1 \end{array} \right) \rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 9 \\ 0 & 20 & 50 & 260 \\ 0 & -1 & 1 & 1 \end{array} \right)$$

$$\rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 9 \\ 0 & -1 & 1 & 1 \\ 0 & 20 & 50 & 260 \end{array} \right) \rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 9 \\ 0 & -1 & 1 & 1 \\ 0 & 0 & 70 & 280 \end{array} \right) \Rightarrow \begin{cases} x + y + z = 9 \\ -y + z = 1 \\ 70z = 280 \end{cases}$$

$$z = \frac{280}{70} = 4 \text{ Kg de uvas; } y = z - 1 = 4 - 1 = 3 \text{ Kg de manzanas.}$$

$$x = 9 - y - z = 9 - 3 - 4 = 2 \text{ Kg de patatas}$$

33

$$\begin{cases} x \rightarrow \text{n}^\circ \text{ puntos } 1^\circ \text{ pregunta} \\ y \rightarrow \text{ " " } 2^\circ \text{ " } \\ z \rightarrow \text{ " " } 3^\circ \text{ " } \end{cases} \begin{cases} x + y + z = 8 \\ y = x + 2 \\ y = z - 1 \end{cases} \begin{cases} x + y + z = 8 \\ -x + y = 2 \\ y - z = -1 \end{cases}$$

$$\left(\begin{array}{ccc|c} 1 & 1 & 1 & 8 \\ -1 & 1 & 0 & 2 \\ 0 & 1 & -1 & -1 \end{array} \right) \rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 8 \\ 0 & 2 & 1 & 10 \\ 0 & 1 & -1 & -1 \end{array} \right) \rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 8 \\ 0 & 1 & -1 & -1 \\ 0 & 2 & 1 & 10 \end{array} \right) \rightarrow$$

$$\rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 8 \\ 0 & 1 & -1 & -1 \\ 0 & 0 & 3 & 12 \end{array} \right) \rightarrow \begin{cases} x + y + z = 8 \\ y - z = -1 \\ 3z = 12 \end{cases} \begin{cases} z = 4 \\ y = -1 + z = 3 = y \\ x = 8 - y - z = 8 - 3 - 4 = 1 = x \end{cases}$$

34

$$\begin{cases} x \rightarrow \text{n}^\circ \text{ hombres} \\ y \rightarrow \text{n}^\circ \text{ mujeres} \\ z \rightarrow \text{n}^\circ \text{ niños} \end{cases} \begin{cases} x + y + z = 20 \\ x + y = 3z \\ y + 1 = x \end{cases} \begin{cases} x + y + z = 20 \\ x + y - 3z = 0 \\ -x + y = -1 \end{cases}$$

$$\left(\begin{array}{ccc|c} 1 & 1 & 1 & 20 \\ 1 & 1 & -3 & 0 \\ -1 & 1 & 0 & -1 \end{array} \right) \rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 20 \\ 0 & 0 & -4 & -20 \\ 0 & 2 & 1 & 19 \end{array} \right) \rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 20 \\ 0 & 2 & 1 & 19 \\ 0 & 0 & -4 & -20 \end{array} \right)$$

$$\begin{cases} x + y + z = 20 \\ 2y + z = 19 \\ -4z = -20 \end{cases} \begin{cases} z = 5 \\ 2y + 5 = 19 \end{cases} \rightarrow \begin{cases} 2y = 14 \rightarrow y = 7 \\ x = 20 - y - z = 20 - 7 - 5 = 8 = x \end{cases}$$

35

$$\begin{cases} x \rightarrow \text{n}^\circ \text{ alumnos } 1^\circ \text{ suc.} \\ y \rightarrow \text{ " " } 2^\circ \text{ suc.} \\ z \rightarrow \text{ " " } 3^\circ \text{ suc.} \end{cases} \begin{cases} x + y + z = 352 \\ z = \frac{1}{4}x \\ x - y = 2z - 2 \end{cases} \begin{cases} x + y + z = 352 \\ x - 4z = 0 \\ x - y - 2z = -2 \end{cases}$$

$$\left(\begin{array}{ccc|c} 1 & 1 & 1 & 352 \\ 1 & 0 & -4 & 0 \\ 1 & -1 & -2 & -2 \end{array} \right) \rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 352 \\ 0 & -1 & -5 & -352 \\ 0 & -2 & -3 & -354 \end{array} \right) \rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 352 \\ 0 & -1 & -5 & -352 \\ 0 & 0 & 7 & 350 \end{array} \right)$$

$$\left. \begin{array}{l} x + y + z = 352 \\ -y - 5z = -352 \\ 7z = 350 \end{array} \right\} \begin{array}{l} z = \frac{350}{7} = 50 \\ y = -5z + 352 = -5 \cdot 50 + 352 = 102 \\ x = 352 - y - z = 352 - 102 - 50 = 200. \end{array}$$

36

$$\left. \begin{array}{l} x \rightarrow \text{n}^\circ \text{cajas de 250g.} \\ y \rightarrow \text{n}^\circ \text{cajas de 500g.} \\ z \rightarrow \text{n}^\circ \text{cajas de 1kg} \end{array} \right\} \begin{array}{l} x + y + z = 60 \\ x = y + 5 \\ 0'25x + 0'5y + z = \frac{1250}{40} \end{array}$$

$$\left. \begin{array}{l} x + y + z = 60 \\ x - y = 5 \\ 25x + 50y + 100z = 3125 \end{array} \right\} \rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 60 \\ 1 & -1 & 0 & 5 \\ 25 & 50 & 100 & 3125 \end{array} \right) \rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 60 \\ 0 & -2 & -1 & -55 \\ 0 & 25 & 75 & 1625 \end{array} \right)$$

$$\rightarrow \left(\begin{array}{ccc|c} 1 & 1 & 1 & 60 \\ 0 & -2 & -1 & -55 \\ 0 & 0 & 125 & 1875 \end{array} \right) \rightarrow \left. \begin{array}{l} x + y + z = 60 \\ -2y - z = -55 \\ 125z = 1875 \end{array} \right\} \begin{array}{l} z = 15 \\ -2y = -55 + 15 \rightarrow y = 20 \\ x = 60 - y - z = 25 = x \end{array}$$